

## **CLAIM AMENDMENTS**

### **Claim Amendment Summary**

#### **Claims pending**

- Before this Amendment: Claims 1-27.
- After this Amendment: Claims 1-27

**Non-Elected, Canceled, or Withdrawn claims:** 3 and 4

**Amended claims:** 1, 13-21, and 25-27

**New claims:** None

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### **Claims:**

1. (Currently Amended) A computer-implemented method for generating a chaos-based pseudo-random sequence ( $X_n$ ) comprising the steps of:

defining a chaotic map for generating a pseudo-random sequence of integer numbers ( $x_n$ ) comprised in a certain interval ( $[0, q]$ );

defining a function ( $H(x)$ ) on a first interval ( $x \in [0, q]$ ) whose inverse has a plurality of branches;

choosing a seed ( $x_0$ ) of said pseudo-random sequence of integer numbers ( $x_n$ ) comprised in said interval ( $[0, q]$ );

generating numbers of said pseudo-random sequence ( $x_n$ );

calculating numbers of a chaos-based pseudo-random sequence (Xn) by applying said function (H(x)) to corresponding integer numbers of said pseudo-random sequence (xn);

storing said chaos-based pseudo-random sequence (Xn) in a circuit;  
and

generating encrypted data on a computer-readable medium by utilizing said chaos-based pseudo-random sequence (Xn) in an encryption application;

wherein said chaotic map is a linear congruential generator defined by:

choosing a first integer number (m);

choosing a second odd integer number (p) greater than the power of 2 raised to said first integer number (2m);

choosing a third integer number (M) much greater than said first integer number (m);

said chaotic map being defined by the following equation:

$$x_{n+1} = \left( \frac{p}{2^m} \cdot x_n \right) \bmod 2^M.$$

2. (Original) The method of claim 1, wherein the inverse of said function (H(x)) has a number of branches equal to the largest bound (q) of said interval ([0, q]).

3. (Canceled)

4. (Canceled)

5. (Original) The method of claim 1, wherein defining said function (H(x)) comprises defining (H(x)) such that it may assume only two values ( ).

6. (Original) The method of claim 5, comprising the steps of:  
representing in binary form said integer numbers (x<sub>n</sub>) of said pseudo-random sequence;  
defining a second integer number k;  
defining said function (H(x)) as the binary sum of the k least significant bits of the binary representation of its argument (x).

7. (Original) The method of claim 5, wherein said chaotic map is a truncated linear congruential generator.

8. (Original) The method of claim 7, wherein said truncated linear congruential generator is defined by:

choosing a first integer number (m);  
choosing a second odd integer number (p) greater than the power of 2 raised to said first integer number (2M);  
choosing a third integer number (M) much greater than said first integer number (m);  
said chaotic map being defined by the following equation:

$$x_{n+1} = \text{trunc}_k \left( \left( \frac{p}{2^m} \cdot x_n \right) \bmod 2^M \right).$$

9. (Original) The method of claim 7, wherein said linear congruential generator is defined by:

choosing a first integer number (m);

choosing a second odd integer number (p) greater than the power of 2 raised to said first integer number (2m);

choosing a third integer number (M) much greater than said first integer number (m);

said chaotic map being defined by the following equations:

$$\begin{cases} y_n = x_n \oplus X_n \\ x_{n+1} = \text{trunc}_k \left( \left( \frac{p}{2^m} \cdot y_n \right) \bmod 2^M \right) \end{cases}$$

10. (Currently Amended) The method according to claim [[4]] 1 wherein said third integer number (M) is greater than or equal to 64.

11. (Previously Presented) The method of claim 6, comprising the steps of:

providing circuit means for storing bit strings representing integer numbers (xn) of said pseudo-random sequence;

providing a shift register (R1) coupled to said circuit means;

storing a seed (x0) in said circuit means;

carrying out cyclically the following operations:

copying in said shift register (R1) a bit string stored in the circuit means representing a current number (xn) of said pseudo-random sequence,

providing k shift commands to said shift register,

generating a bit ( $X_n$ ) of said chaos-based pseudo-random bit sequence by summing modulo 2 the  $k$  bits output by said shift register,

generating a bit string representing a successive number ( $x_{n+1}$ ) of said pseudo-random sequence by summing up the bit string currently stored in said shift register ( $R_1$ ) and the bit string representing said current number ( $x_n$ ),

storing in the circuit means the bit string representing said successive number ( $x_{n+1}$ ).

12. (Previously Presented) The method of claim 6, comprising the steps of:

providing circuit means for storing bit strings representing integer numbers ( $x_n$ ) of said pseudo-random sequence;

providing a register  $[(R_1)]$  coupled to said circuit means;

storing a seed ( $x_0$ ) in said circuit means;

carrying out cyclically the following operations:

copying in said register a bit string stored in the circuit means representing a current number ( $x_n$ ) of said pseudo-random sequence,

generating a bit ( $X_n$ ) of said chaos-based pseudo-random bit sequence by summing modulo 2 the  $k$  least significant bits of the bit string stored in said register,

generating a bit string representing a successive number ( $x_{n+1}$ ) of said pseudo-random sequence by summing up the bit string representing said current number ( $x_n$ ) and the bit string obtained eliminating the  $k$  least significant bits of the bit string stored in said register,

storing in the circuit means the bit string representing said successive number ( $x_{n+1}$ ).

13. (Currently Amended) A generator of chaos-based pseudo-random bit sequences operable in an encryption application, comprising:

circuit means for storing bit strings representing integer numbers ( $x_n$ ) of said pseudo-random sequence;

a register coupled to said circuit means;

an adder modulo 2 summing the  $k$  least significant bits of the of the bit string stored in said register, generating a bit ( $X_n$ ) of said chaos-based pseudo-random bit sequence; [[ and]]

a second adder summing up the bit string representing said current number ( $x_n$ ) and the bit string obtained eliminating the  $k$  least significant bits of the bit string stored in said register; and

a data generator for generating encrypted data on a computer-readable medium based on said pseudo-random sequence.

14. (Currently Amended) A generator of chaos-based pseudo-random bit sequences operable in an encryption application, comprising:

circuit means for storing bit strings representing integer numbers ( $x_n$ ) of said pseudo-random sequence;

a shift register coupled to said circuit means;

a command circuit generating shift commands for said shift register;

second circuit means  $[(R2)]$  for storing the bits output by said shift register;

an adder modulo 2 summing the bits stored in said second circuit means, generating a bit ( $X_n$ ) of said chaos-based pseudo-random bit sequence;

a second adder summing up the bit strings currently stored in said shift register and in said first circuit means, generating a bit string representing a successive number ( $x_{n+1}$ ) of said pseudo-random sequence; and

a data generator for generating encrypted data on a computer-readable medium based on said pseudo-random sequence.

15. (Currently Amended) A method, comprising:

generating a first pseudo-random value with a chaotic map;

generating a first chaos-based pseudo-random value as a function of the first pseudo-random value, the function having an inverse with a plurality of branches;

storing the first chaos-based pseudo-random value in a circuit; and

encrypting data using the stored first chaos-based pseudo-random value  
~~utilizing the first chaos-based pseudo-random value in an encryption application.~~

16. (Currently Amended) The method of claim 15 wherein generating the first pseudo-random value comprises generating the first pseudo-random value within a finite interval of values.

17. (Currently Amended) The method of claim 15 wherein:

generating the first pseudo-random value comprises generating the first pseudo-random value within a finite interval of values, the finite interval having an upper bound; and

the inverse of the function has a number of branches, the number being equal to the upper bound of the finite interval.

18. (Currently Amended) The method of claim 15, further comprising generating the first pseudo-random value from a seed value.

19. (Currently Amended) The method of claim 15, further comprising generating the first pseudo-random value from a previously generated pseudo-random value.

20. (Currently Amended) The method of claim 15, further comprising generating the first pseudo-random value from a previous chaos-based pseudo-random value.

21. (Currently Amended) The method of claim 15, further comprising:  
generating a second pseudo-random value from the first pseudo-random value with the chaotic map; and  
generating a second chaos-based pseudo-random value as the function of the second pseudo-random value.



22. (Previously Presented) The method of claim 15 wherein the chaotic map comprises a linear congruential generator.

23. (Previously Presented) The method of claim 15 wherein the chaotic map comprises a truncated linear congruential generator.

24. (Previously Presented) The method of claim 15 wherein the function comprises an exclusive or function.

25. (Currently Amended) The method of claim 15 wherein the function comprises an exclusive or function of multiple bits of the first pseudo-random value.

26. (Currently Amended) A circuit, comprising:  
a first generator operable to generate a first pseudo-random value with a chaotic map;

a second generator coupled to the first generator and operable to generate a first chaos-based pseudo-random value ~~operable to be used in an encryption application and~~ as a function of the first pseudo-random value, the function having an inverse with a plurality of branches; [[ and]]

a memory for storing the first chaos-based pseudo-random value; and  
an encrypter coupled to the memory and operable to encrypt data with the first chaos-based pseudo-random value.

27. (Currently Amended) A system, comprising:  
a circuit, comprising,  
a first generator operable to generate a first pseudo-random value with a chaotic map;[[ and]]  
a second generator coupled to the first generator and operable to generate a first chaos-based pseudo-random value ~~operable to be used in an encryption application~~ and as a function of the first pseudo-random value, the function having an inverse with a plurality of branches;[[ and]]  
a memory for storing the first chaos-based pseudo-random value; and  
an encrypter coupled to the memory and operable to encrypt data with the first chaos-based pseudo-random value.